## Precalculus

## Lesson 10.3: The Ellipse

Mrs. Snow, Instructor
THE ELLIPSE BECAME INCREASINGLY ECCENTRIC.



GRANT SNIDER
Ellipse: the collection, or locus, of all points in the plane, the sum of whose distances from two fixed points, called the foci, is constant.

## Major axis it's the x-axis:

Equation of an Ellipse: Center at ( $\mathbf{0}, \mathbf{0}$ ); Major Axis along the $\boldsymbol{x}$-Axis
An equation of the ellipse with center at $(0,0)$, foci at $(-c, 0)$ and $(c, 0)$, and vertices at $(-a, 0)$ and $(a, 0)$ is

$$
\begin{equation*}
\frac{x^{2}}{a^{2}}+\frac{y^{2}}{b^{2}}=1, \quad \text { where } a>b>0 \text { and } b^{2}=a^{2}-c^{2} \tag{2}
\end{equation*}
$$

Major axis is the $y$-axis:
Equation of an Ellipse; Center at ( 0,0 ); Major Axis along the $\boldsymbol{y}$-Axis
An equation of the ellipse with center at $(0,0)$, foci at $(0,-c)$ and $(0, c)$, and vertices at $(0,-a)$ and $(0, a)$ is

$$
\begin{equation*}
\frac{x^{2}}{b^{2}}+\frac{y^{2}}{a^{2}}=1 \quad \text { where } a>b>0 \text { and } b^{2}=a^{2}-c^{2} \tag{3}
\end{equation*}
$$

Finding an equation of an Ellipse


## Analyze the Equation of an Ellipse

| Analyze (find the center foci and vertices) |
| :---: | :---: | :---: | :---: | :---: |
| $\frac{x^{2}}{25}+\frac{y^{2}}{9}=1$ |

Find an equation of the ellipse having one focus at ( 0,2 ) and vertices at $(0,-3)$ and $(0,3)$. Graph.


Ellipses with centers at (h, k)

| Equations of an Ellipse: Center at ( $\boldsymbol{h}, \boldsymbol{k}$ ); Major Axis Parallel to a Coordinate Axis |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Center | Major Axis | Foci | Vertices | Equation |
| ( $h$, k) | Parallel to the $x$-axis | $(h+c, k)$ | $(h+a, k)$ | $\frac{(x-h)^{2}}{a^{2}}+\frac{(y-k)^{2}}{b^{2}}=1,$ |
|  |  | $(h-c, k)$ | $(h-a, k)$ | $a>b>0$ and $b^{2}=a^{2}-c^{2}$ |
| ( $h, k$ ) | Parallel to the $y$-axis |  |  | $\frac{(x-h)^{2}}{b^{2}}+\frac{(y-k)^{2}}{a^{2}}=1,$ |
|  |  | $(h, k-c)$ | $(h, k-a)$ | $a>b>0$ and $b^{2}=a^{2}-c^{2}$ |

Find an equation of an ellipse with center at $(2,-3)$, one focus at $(3,-3)$, and one vertex at $(5,-3)$. Graph



The whispering gallery in the Museum of Science and Industry in Chicago is 47.3 feet long. The distance from the center of the room to the foci is 20.3 feet. Find an equation that describes the shape of the room. How high is the room at its center?

