

Precalculus

Inverse: A mathematical operation that is the opposite effect of another operation. The operation undoes what the first operation did! Some examples of inverse operations include addition and subtraction and multiplication and division.

In 5.2 we studied inverse functions. If a function is one-to-one it has an inverse function (one function undoes the other). To make a function one-to-one, place restrictions on the domain. While trig functions are of course functions, they are not all one-to-one. By placing limits on the domain, a trig function may be forced into being one-to-one.

Remember to find the inverse simply switch the x and y values; x is y and y is x. Switch the domain and range.



Inverse Sine Function: sin^{-1} is also known as <u>arcsine</u> and written as <u>arcsin</u>

Remember, that inverses undo one another, so if I take the inverse sine of sine, *OR*! the sine of the inverse sine, the operation is undone!

Finding the exact value of an inverse sine function; we are looking for an angle θ , $\frac{-\pi}{2} \le \theta \le \frac{\pi}{2}$



Approximate values of inverse sine functions may be found using a calculator. Express the answer in radians rounded to 2 decimal places. What quadrant will you find these angles?

$sin^{-1}\frac{1}{3}$	$sin^{-1}\left(-\frac{1}{4}\right)$

For composite functions, the domain is dependent upon the domain restrictions of the inner function. This is crucial when determining the value of a composite function where the inner function is outside the domain restrictions.

In the terms of the sine function and its inverse, we have the following properties:

$$f^{-1}(f(x)) = \sin^{-1}(\sin x) = x$$
 where $-\frac{\pi}{2} \le x \le \frac{\pi}{2}$
 $f(f^{-1}(x)) = \sin(\sin^{-1}x) = x$ where $-1 \le x \le 1$

Find the exact value of composite functions:

- Can we use composite function rules from above?
- Work from the inside out.
- When sine is the inside function, solve for $sin \theta$,
- Then deal with the inverse function, *make sure you pay attention to the domain of x*!!!



$sin^{-1}(sin\frac{7\pi}{6})$	$\sin(\sin^{-1}(5))$	$\sin(\sin^{-1}(1.8))$

Same process may be used for cosine:

Inverse Cosine Function: cos^{-1} also called <u>arcosine</u> and written as <u>arcos</u>



In the terms of the cosine function and its inverse, we have the following properties:

$$f^{-1}(f(x)) = \cos^{-1}(\cos x) = x$$
 where $0 \le x \le \pi$
 $f(f^{-1}(x)) = \cos(\cos^{-1} x) = x$ where $-1 \le x \le 1$

- Can we use composite function rules from above?
- Work from the inside out.
- When cosine is the inside function, solve for $cos\theta$,
- Then deal with the inverse function, make sure you pay attention to the domain of x!!!





Inverse Tangent Function: tan^{-1} also called <u>arctangent</u> and written as <u>arctan</u>

EXAMPLE Evaluate the inverse tangent functions; find θ for $\frac{-\pi}{2} < \theta < \frac{\pi}{2}\theta$



In the terms of the tangent function and its inverse, we have the following properties:

$$f^{-1}(f(x)) = \tan^{-1}(\tan x) = x \quad \text{where } -\frac{\pi}{2} < x < \frac{\pi}{2}$$
$$f(f^{-1}(x)) = \tan(\tan^{-1} x) = x \quad \text{where } -\infty < x < \infty$$

Precalculus Lesson 7.2: The Inverse Trigonometric Functions (continued) Mrs. Snow, Instructor

Composing a Trig Function

What???? Evaluate a trig function involving inverse functions.



Write a Trigonometric expression as an Algebraic Expression: Look back to the first example. What is the first step?

$\sin(tan^{-1}u)$	