## Calculus

Lesson 8.5: Using Partial Fraction
Decomposition to Integrate
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In this lesson we will review a procedure for decomposing a rational function into simpler rational functions to which you can apply the basic integration formulas.

## A review of partial fraction decomposition:

1. Distinct Linear Factors
$\frac{P(x)}{Q(x)}=\frac{A_{1}}{x-a_{1}}+\frac{A_{2}}{x-a_{2}}+\cdots+\frac{A_{n}}{x-a_{n}}$
2. Repeated Linear Factors
$\frac{A_{1}}{x-a}+\frac{A_{2}}{(x-a)^{2}}+\cdots+\frac{A_{n}}{(x-a)^{n}}$
3. Distinct Quadratic Factors
$\frac{A x+B}{a x^{2}+b x+c}$

Finding a Partial Fraction Decomposition
$\frac{x-13}{2 x^{2}-7 x+3}$

## Finding an Integral with Partial Fractions

- Find
$\int \frac{3 x^{4}+1}{x^{2}-1} d x$


## Finding Three Partial Fractions

- Find the general solution to
$\frac{d y}{d x}=\frac{6 x^{2}-8 x-4}{\left(x^{2}-4\right)(x-1)}$

