Precalculus

Lesson 8.5: Simple Harmonic Motion and combining Waves
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Repetitive motion as seen in the rising and falling of the tide, the changing of the seasons year after year, or sunrise and sunset are all examples of periodic behavior. Trigonometric functions are ideally suited for modeling periodic behavior.

cycle: one complete vibration or motion of an object is a cycle

amplitude: |a| the distance from the object's rest position to its point of greatest displacement

period: $T=\frac{2\pi}{\omega}$; time required to complete one complete cycle frequency: $f=\frac{\omega}{2\pi}$ number of cycles per unit of time

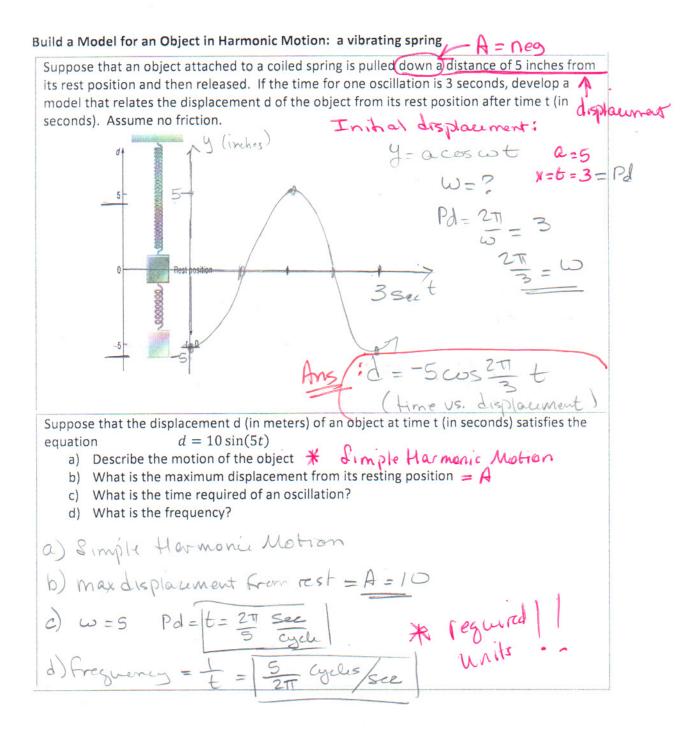
simple harmonic motion: an object is considered to be in simple harmonic motion if the displacement **d** of an object at time **t** can be modeled by:

 $d = a \sin \omega t$ or $d = a \cos \omega t$

Thoughts: consider the equation that models harmonic motion at time 0, the starting point.

solve for displacement: $d = a \sin \omega t$ at t = 0, No Initial $d = a \sin \omega \Rightarrow d = 0 \ge 7$ displacement $d = a \cos \omega t$ at time = 0 $d = a \cos \omega t \Rightarrow d = a \Leftrightarrow Initial displacement$

So, one equation works for situations where there is no displacement at initial conditions and the other equations is applicable for initial conditions that have a displacement.



- Period

A person is seated on a Ferris wheel of radius 100 ft that makes one rotation every 30 s. The center of the wheel is 105 ft above the ground. Find and graph a function to represent the person's height above the ground at any time t of a 2-minute ride. Assume uniform speed from the beginning to the end of the ride and that the person is at the level of the center of the wheel and headed up when the ride begins.

(hint: Make a table of time vs. height, graph and build an equation based on the graph.)

