

In 1-2, find the slope of the tangent line to the graph of the function at the given point.

1. $f(x) = 8 - x^2$, $(2, 4)$
2. $h(t) = t^2 + 5$, $(-3, 14)$

In 3-5, find the derivative by the limit process.

3. $f(x) = 1 - 2x^2$
4. $f(x) = \frac{1}{x+1}$
5. $f(x) = \frac{2}{\sqrt{x}}$

In 6-7, find an equation of the tangent line to the graph of f at the given point.

6. $f(x) = x^3$, $(-2, -8)$
7. $f(x) = \sqrt{x-6}$, $(10, 2)$

In 8-9, use the alternative form of the derivative to find the derivative at $x=c$ (if it exists).

8. $g(x) = 2x(x-1)$, $c = 1$
9. $g(x) = \frac{3}{x}$, $c = 2$

In 10, find the derivatives from the left and from the right at $x=2$ (if they exist). Is the function differentiable at $x=2$?

10. $f(x) = |x-2|$

In 11-18, find the derivative of the function.

11. $y = x^8$
12. $f(x) = \sqrt[7]{x}$
13. $f(x) = 2x^5 - x^3 + 5x$
14. $y = x^2 - \frac{1}{4} \sin x$
15. $y = \frac{3}{(-2x)^3} + 3 \cos x$
16. $f(x) = x^3 + 7 - 5x^{-2}$
17. $f(x) = 4x + \frac{2}{x^2}$
18. $y = 3x(2x^2 + 1)$

In 19-20, find an equation of the tangent line to the graph of f at the given point.

$$19. f(x) = -\frac{1}{2} + \frac{5}{3}x^3, \left(0, -\frac{1}{2}\right)$$

$$20. y = 2x^3 - x, (1, 1)$$

In 21-22, determine the point(s) (if any) at which the graph of the function has a horizontal tangent line.

$$21. y = 2x^4 - 16x^2 + 3$$

$$22. y = 4x^2 + 1$$

In 23, use the position function

$$s(t) = -16t^2 + s_0 \text{ for free-falling objects.}$$

23. A silver dollar is dropped from the top of a building that is 862 feet tall.

- Determine the position and velocity functions for the coins.
- Determine the average velocity on the interval $[1, 2]$.
- Find the instantaneous velocities when $t=1$ and $t=2$.
- Find the time required for the coin to reach ground level.
- Find the velocity of the coin at impact.

In 24-32, find the derivative using the product or the quotient rule.

$$24. f(x) = (x^2 - 1)(x^3 - 2x)$$

$$25. f(x) = 2x^2 \cos x$$

$$26. g(x) = \frac{\sin x}{x^3}$$

$$27. g(t) = \frac{t^2 - 3}{2t + 5}$$

$$28. f(x) = \frac{3 - x - x^3}{2x^2 + 1}$$

$$29. f(x) = \frac{1 - \frac{3}{x}}{x + 2}$$

$$30. f(x) = -x + 2 \tan x$$

$$31. f(x) = 2x \cos x + x^2 \sin x$$

$$32. g(t) = \sqrt[3]{t} + 5 \sec t$$

In 33-35, Find the second derivative of the function.

$$33. f(x) = \frac{x^2 + 4x - 1}{3x}$$

$$34. f(x) = 3 \cos x$$

$$35. f(x) = \frac{2x}{x - 1}$$

In 36-38, find $f'(x)$ and $f'(c)$

36.

$$f(x) = (x^2 - 3x)(2x^3 + 3x + 1) \quad c = 1$$

37.

$$f(x) = \frac{x^2 - 4}{x - 1} \quad c = 2$$

38.

$$f(x) = x \cos x \quad c = \frac{\pi}{2}$$