

Even and Odd Functions

Think back to algebra, how do we determine the degree of a function?

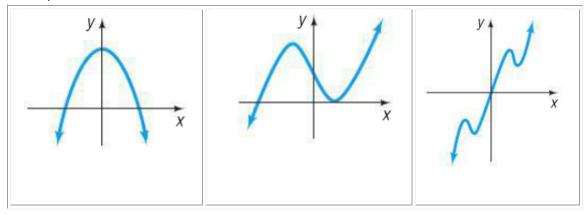
- > A function is **even** if and only if its graph is symmetric with respect to the y-axis.
- Whenever the point (x, y) is on the graph of f then the point (-x, y) is also on the

$$► f(-x) = f(x)$$

- > A function is **odd** if and only if its graph is symmetric with respect to the origin.
- For every point (x, y) on the graph, the point (-x, -y) is also on the graph.

▶
$$f(-x) = -f(x)$$

Identify if the function is even, odd or neither



Even or Odd?

$f(x) = x^2 - 5$	$g(x) = x^3 - 1$	$h(x) = 5x^3 - x$

Increasing, Decreasing, or Constant?

Functions are often used to model changing quantities. Where the slope is positive we say it is increasing, and where the slope is negative we say it is decreasing. Horizontal? It is neither increasing nor decreasing; it is considered constant.

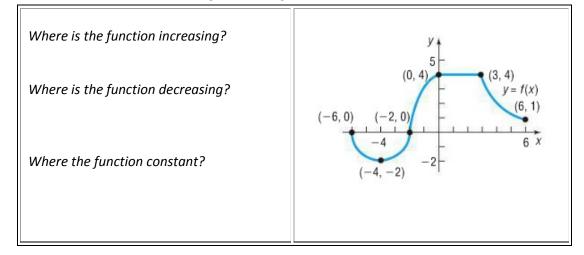
Definition:

A function f is **increasing** on an open interval I if, for any choice of x_1 and x_2 in I, with $x_1 < x_2$, we have $f(x_1) < f(x_2)$.

A function f is **decreasing** on an open interval I if, for any choice of x_1 and x_2 in I, with $x_1 < x_2$, we have $f(x_1) > f(x_2)$.

* The open interval (a, b) consists of all real numbers x for which a < x < b.

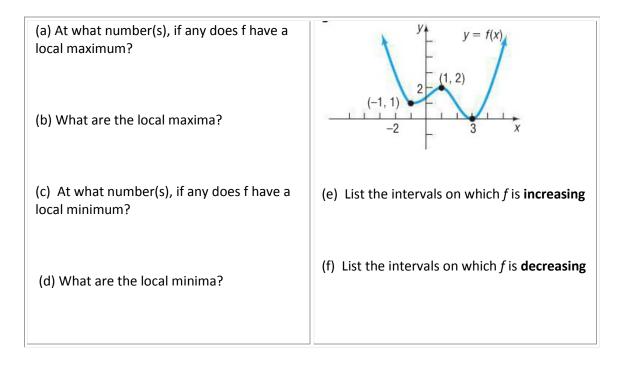
Determine where a function is increasing, decreasing or constant:



A function f has a **local maximum** at c if there is an open interval I containing c so that for all x in I, $f(x) \le f(c)$. We call f(c) a **local maximum value of f**.

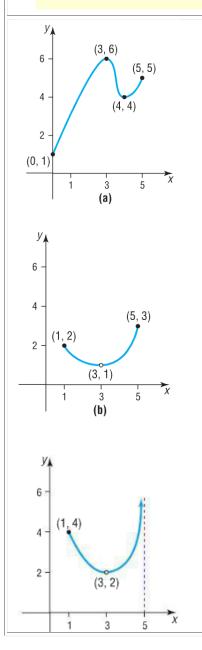
A function f has a **local minimum** at c if there is an open interval I containing c so that, for all x in I, $f(x) \ge f(c)$. We call f(c) a **local minimum value of f**.

Note: Local maximum and minimum occur in open intervals.



Extreme Value Theorem

If f is a continuous function^{*} whose domain is a closed interval [a, b], then f has an absolute maximum and an absolute minimum on [a, b].

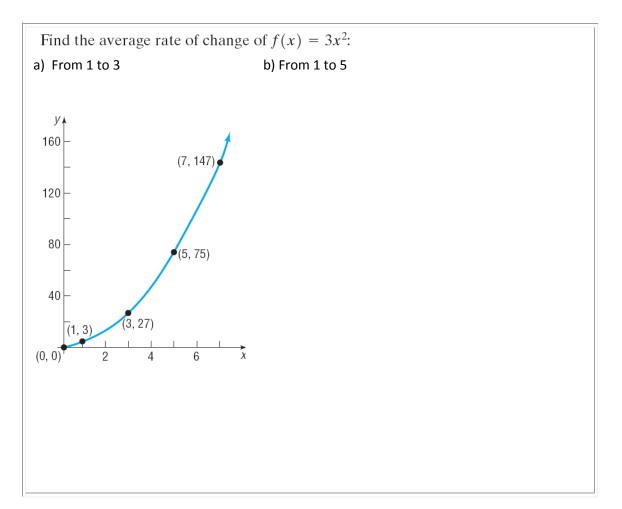


Calculators often help in determining absolute maxima and minima and find where and find where a function is decreasing or increasing.

Use a graphing utility to graph $f(x) = 6x^3 - 12x + 5$ for -2 < x < 2. Approximate where f has a local maximum and where f has a local minimum.

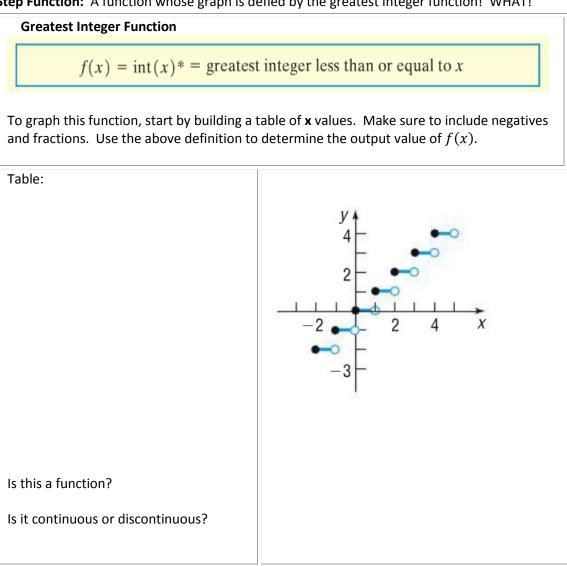
Average Rate of Change
Average rate of change
$$= \frac{\Delta y}{\Delta x} = \frac{f(b) - f(a)}{b - a} = m_{sec}$$

When a function is graphed and the *average rate of change* is calculated, graphically a line drawn between f(a) and f(b) is called a **secant line**. The *average rate of a secant line is designated as:* m_{sec}



Lesson 2.4

Step Function: A function whose graph is defied by the greatest integer function! WHAT!



continuous: a function in which its graph has no gaps of holes in it. It can be drawn without lifting your pencil from the paper.

discontinuous: a function in which its graph has holes or breaks in the curve. To draw this graph you would need to lift your pencil off the paper.

