## Precalculus

Lesson: 2.1 What is a Function and Lesson 2.2: Graphs of Functions
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## Lesson 2.1

## "Working Definition" of Function"

A function is a relation for which each value from the set of the first components (independent variable) of the ordered pairs is associated with exactly one value from the set of second components (dependent variable) of the ordered pair. When we think of function equations, for every input $x$ there exactly one output value of $y$. There are no $x$ repeaters.


Determine whether the equation is a function.

$$
x=y^{2}-1
$$

$$
y=\frac{1}{2} x-3
$$

For the given function evaluate: $\quad f(x)=2 x^{2}-3 x$ for:
(a) $f(3)$
(b) $f(x)+f(3)$
(c) $3 f(x)$
(d) $f(-x)$
(e) $-f(x)$
(f) $f(3 x)$
(g) $f(x+3)$
$\propto(\mathrm{h}) \frac{f(x+h)-f(x)}{h} \quad h \neq 0$

## Domain of a Function

Three points to remember!!

1. Denominator cannot equal zero
2. Anything under a square root has to be greater than or equal to zero, what if the square root is located in a denominator?
3. If no domain is specified, then the domain will be taken to be the largest set of real numbers for which the equation defines a real number.

Find the domain: Remember interval notation only!!!

| $f(x)=\frac{x+4}{x^{2}-2 x-3}$ | $g(x)=x^{2}-9$ | $h(x)=\sqrt{3-2 x}$ |
| :--- | :--- | :--- |

If we have two functions, we can use different techniques to combine them into one function
If $f$ and $g$ are functions:
The sum $\boldsymbol{f}+\boldsymbol{g}$ is the function defined by

| $(f+g)(x)=f(x)+g(x)$ |
| :---: |
| Domain: $\boldsymbol{f} \cap \boldsymbol{g}$ |
| The difference $\boldsymbol{f}-\boldsymbol{g}$ is the function defined by |
| $(f-g)(x)=f(x)-g(x)$ |
| Domain: $\boldsymbol{f} \cap \boldsymbol{g}$ |
| The product $\boldsymbol{f} \cdot \boldsymbol{g}$ is the function defined by |
| $\quad(f \cdot g)(x)=f(x) \cdot g(x)$ |
| Domain: $\boldsymbol{f} \cap \boldsymbol{g}$ |
| The quotient $\frac{\boldsymbol{f}}{\boldsymbol{g}}$ is the function defined by |
| Domain: $\{\boldsymbol{x} \mid \boldsymbol{g}(\boldsymbol{x}) \neq \mathbf{0}\}, \cap$ domain of $\boldsymbol{f} \cap$ domain of $\boldsymbol{g}$ |

## Combinations of Functions and Their Domains:

$$
\text { Let } f(x)=2 x^{2}+3 \quad \text { and } g(x)=4 x^{3}+1
$$

1. Find the functions $(f+g)(x),(f-g)(x)$, $(f \cdot g)(x)$, and $\left(\frac{f}{g}\right)(x) \quad$ and determine their domains.

## Lesson 2.2-Graphs of Functions

Sometimes a visual representation, a graph, of a relationship is easier to understand.

The Vertical Line Test is a technique to verify if a graph represents a function.
Vertical Line Test: The graph of a function cannot contain two points with the same $x$ coordinate and different y-coordinates.

Identify the graphs that represent a function and the domains for all:


(a) What are $f(0), f\left(\frac{3 \pi}{2}\right)$, and $f(3 \pi)$ ?
(b) What is the domain of $f$ ?
(c) What is the range of $f$ ?
(d) List the intercepts. (Recall that these are the points, if any, where the graph ${ }^{1}$ crosses or touches the coordinate axes.)
(e) How many times does the line $y=2$ intersect the graph?
(f) For what values of $x$ does $f(x)=-4$ ?
(g) For what values of $x$ is $f(x)>0$ ?

## Obtaining Information about the Graph of a Function

Consider the function: $f(x)=\frac{x+1}{x+2}$
(a) Find the domain of $f$.
(b) Is the point $\left(1, \frac{1}{2}\right)$ on the graph of $f$ ?
(c) If $x=2$, what is $f(x)$ ? What point is on the graph of $f$ ?

## Average Cost Function

The average cost $\bar{C}$ of manufacturing $x$ computers per day is given by the function

$$
\bar{C}(x)=0.56 x^{2}-34.39 x+1212.57+\frac{20,000}{x}
$$

Determine the average cost of manufacturing:
(a) 30 computers in a day
(b) 40 computers in a day
(c) 50 computers in a day
(d) Graph the function $\bar{C}=\bar{C}(x), 0<x \leq 80$.
(e) Create a TABLE with TblStart $=1$ and $\Delta \mathrm{Tbl}=1$. Which value of $x$ minimizes the average cost?

