## Precalculus Lesson 8.5: Simple Harmonic Motion and combining Waves Mrs. Snow, Instructor

Repetitive motion as seen in the rising and falling of the tide, the changing of the seasons year after year, or sunrise and sunset are all examples of periodic behavior. Trigonometric functions are ideally suited for modeling periodic behavior.

**cycle** – one complete vibration or motion of an object is a cycle a.k.a. period **simple harmonic motion** – an object is considered to be in simple harmonic motion if the displacement **d** of an object at time **t** can be modeled by:

 $d = a \sin\omega t \quad or \quad d = a \cos\omega t$ amplitude - |a| maximum displacement of the object
period -  $\frac{2\pi}{\omega}$  time required to complete one complete cycle
frequency -  $f = \frac{\omega}{2\pi}$  number of cycles per unit of time

Thoughts: consider the equations that model harmonic motion at time equal to 0, at the starting point.

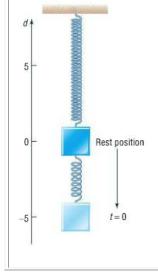
 $d = a \sin\omega t \quad at \ t = 0$   $d = a \sin 0 = 0 \quad or \ at \ time = 0, \qquad displacement = 0$   $d = a \cos\omega t \quad at \ time = 0$  $d = a \cos 0 \quad or \ at \ time = 0, \qquad displacement = a$ 

So, one equation works for situations where there is no displacement at initial conditions and the other equations is applicable for initial conditions that have a displacement.

A Vibrating Spring

An object is attached to a coiled spring and is pulled down a distance of 5 inches from its rest position and then released. The time for one oscillation is 3 seconds. Develop a model that relates the displacement d of the object from it rest position after time t in seconds. Translation: write an equation for this situation. Assume no friction.

Also, find the amplitude, period, and frequency of the motion of the mass. Sketch the graph of the displacement of the mass.



Suppose that the displacement d (in meters) of an object at time t (in seconds) satisfies the equation  $d = 10 \sin(5t)$ 

- a) Describe the motion of the object
- b) What is the maximum displacement from its resting position
- c) What is the time required of an oscillation?
- d) What is the frequency?

## A Ferris wheel Problem

A person is seated on a Ferris wheel of radius 100 ft that makes one rotation every 30 s. The center of the wheel is 105 ft above the ground. Find and graph a function to represent the person's height above the ground at any time t of a 2-min ride. Assume uniform speed from the beginning to the end of the ride and that the person is at the level of the center of the wheel and headed up when the ride begins. (hint: Make a table of time vs. height, graph and build an equation based on the graph.)

