## Precalculus

## Lesson 8.4: Area of a Triangle

Mrs. Snow, Instructor

If we know two sides of a triangle and the included triangle we may apply the general formula for the area of a triangle (SAS).

$$
\sin C=\frac{h}{a}
$$

solving for h :

$$
h=\mathrm{a} \sin C
$$

so area is:


$$
K=\frac{1}{2} b h=\frac{1}{2} a b \sin C
$$

To find area of a triangle knowing SAS

$$
\begin{aligned}
K & =\frac{1}{2} a b \sin C \\
K & =\frac{1}{2} a c \sin B \\
K & =\frac{1}{2} \sin A
\end{aligned}
$$

From the law of cosines comes Heron's Formula that may be used to find the area of a triangle if only given the lengths of the three sides (SSS):
For a triangle with sides of lengths $a, b$, and $c$, it will have a semiperimeter of:

$$
s=\frac{1}{2}(a+b+c)
$$

the area of the triangle is:

$$
K=\sqrt{s(s-a)(s-b)(s-c)}
$$

Find the area of a triangle whose sides are
$a=4, b=5, c=7$

Find the area of the triangle:


