Precalculus

Lesson 8.4: Area of a Triangle

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If we know two sides of a triangle and the included triangle we may apply the general formula for the area of a triangle (SAS).

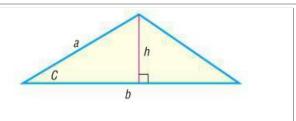


solving for h:

$$h = a \sin C$$

so area is:

$$K = \frac{1}{2}bh = \frac{1}{2}ab\sin C$$



To find area of a triangle knowing SAS

$$K = \frac{1}{2}ab \sin C$$

$$K = \frac{1}{2}ac \sin B$$

$$K = \frac{1}{2}\sin A$$

From the law of cosines comes **Heron's Formula** that may be used to find the area of a triangle if only given the lengths of the three sides (SSS):

For a triangle with sides of lengths a, b, and c, it will have a **semiperimeter** of:

$$s=\frac{1}{2}(a+b+c)$$

the area of the triangle is:

$$K = \sqrt{s(s-a)(s-b)(s-c)}$$

Find the area of a triangle whose sides are

$$a = 4, b = 5, c = 7$$

