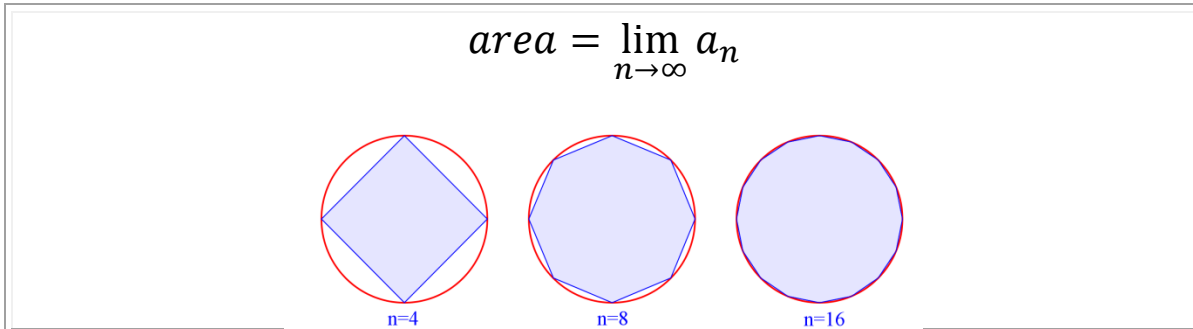


Precalculus

Lesson 14.1: Finding Limits Using Tables and Graphs

Mrs. Snow, Instructor

The title of this chapter is “Limits: A Preview of Calculus.” The central idea behind calculus is the concept of a **limit**. Calculus is used in modeling numerous real-life phenomena, particularly situations that involve change or motion. To better understand limits let’s look back at the Greeks some 2500 years ago and how they used the “method of exhaustion” to find areas. To find the area of a circle for example, the Greeks inscribed a polygon inside the curved region. As the number of sides of the polygon increases, the polygon’s area approaches the area of the circle. In other words:



Definition of a Limit:

We write:

$$\lim_{x \rightarrow a} f(x) = L$$

We say: The limit of $f(x)$, as x approaches a , equals L .

We mean: as x gets closer and closer to a , the y value gets closer and closer to L .

Finding a Limit From a Table

Find the limit of

$$\lim_{t \rightarrow 0} \frac{\sqrt{t^2 + 9} - 3}{t^2}$$

FROM THE RIGHT

t	0.5	0.1	0.01	0.001
f(x)				

FROM THE LEFT

t	-0.5	-0.1	-0.01	-0.001
f(x)				

Find the limit from a table and estimate using the graph of (what are the restrictions?):

$$\lim_{x \rightarrow 1} \frac{x - 1}{x^2 - 1}$$

Limits That Fail to Exist: A Function With a Jump

$$H(t) = \begin{cases} 0 & \text{if } t < 0 \\ 1 & \text{if } t \geq 0 \end{cases}$$

Limits That Fail to Exist: A Function That Oscillates

$$\lim_{x \rightarrow 0} \sin \frac{\pi}{x}$$

Limits That Fail to Exist: A Function with a Vertical Asymptote

$$\lim_{x \rightarrow 0} \frac{1}{x^2}$$

One Sided Limits

Left Sided Limit

$$\lim_{x \rightarrow a^-} f(x) = L$$

Right Sided Limit

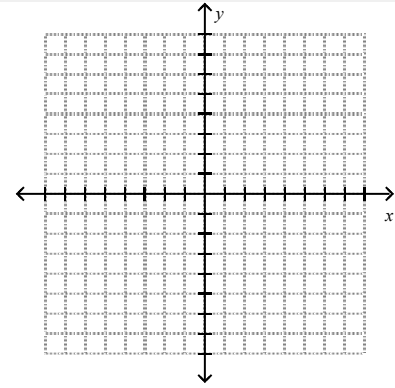
$$\lim_{x \rightarrow a^+} f(x) = L$$

Very Important!!!!

$$\lim_{x \rightarrow a} f(x) = L \text{ if and only if } \lim_{x \rightarrow a^-} f(x) = L \text{ AND } \lim_{x \rightarrow a^+} f(x) = L$$

Limits From a Graph: A Piecewise-Defined Function

$$f(x) = \begin{cases} 2x^2 & \text{if } x < 1 \\ 4 - x & \text{if } x \geq 1 \end{cases}$$



Find :

$$\lim_{x \rightarrow 1^-} f(x)$$

$$\lim_{x \rightarrow 1^+} f(x)$$

$$\lim_{x \rightarrow 1} f(x)$$

$$g(x) = \begin{cases} x^2, & x \neq 2 \\ 1, & x = 2 \end{cases}$$

find $\lim_{x \rightarrow 2} g(x)$

