

Homework 14.2

1. Suppose that

$$\lim_{x \rightarrow a} f(x) = -3$$

$$\lim_{x \rightarrow a} g(x) = 0$$

$$\lim_{x \rightarrow a} h(x) = 8$$

Find the value of the given limit, if it exists.

a) $\lim_{x \rightarrow a} [f(x) + h(x)]$

b) $\lim_{x \rightarrow a} [f(x)]^3$

c) $\lim_{x \rightarrow a} \sqrt[3]{h(x)}$

d) $\lim_{x \rightarrow a} \frac{1}{f(x)}$

e) $\lim_{x \rightarrow a} \frac{f(x)}{h(x)}$

f) $\lim_{x \rightarrow a} \frac{g(x)}{f(x)}$

g) $\lim_{x \rightarrow a} \frac{f(x)}{g(x)}$

h) $\lim_{x \rightarrow a} \frac{2f(x)}{h(x) - f(x)}$

2. The graphs of f and g are given. Use them to evaluate each limit, if it exists.

(a) $\lim_{x \rightarrow 2} [f(x) + g(x)]$

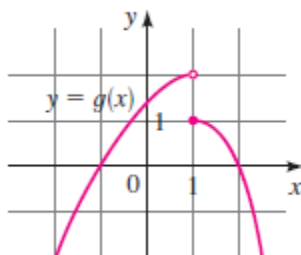
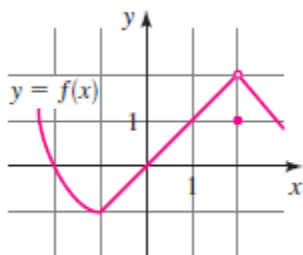
(b) $\lim_{x \rightarrow 1} [f(x) + g(x)]$

(c) $\lim_{x \rightarrow 0} [f(x)g(x)]$

(d) $\lim_{x \rightarrow -1} \frac{f(x)}{g(x)}$

(e) $\lim_{x \rightarrow 2} x^3 f(x)$

(f) $\lim_{x \rightarrow 1} \sqrt{3 + f(x)}$



#3-14 Evaluate the limit, if it exists.

3. $\lim_{x \rightarrow 4} (5x^2 - 2x + 3)$

7. $\lim_{x \rightarrow 2} \frac{x^2 + x - 6}{x - 2}$

11. $\lim_{h \rightarrow 0} \frac{(3+h)^{-1} - 3^{-1}}{h}$

4. $\lim_{x \rightarrow -1} \frac{x - 2}{x^2 + 4x - 3}$

8. $\lim_{x \rightarrow 1} \frac{x^3 - 1}{x^2 - 1}$

12. $\lim_{x \rightarrow -4} \frac{\frac{1}{4} + \frac{1}{x}}{4 + x}$

5. $\lim_{x \rightarrow 1} \left(\frac{x^4 + x^2 - 6}{x^4 + 2x + 3} \right)^2$

9. $\lim_{h \rightarrow 0} \frac{(2+h)^3 - 8}{h}$

13. $\lim_{x \rightarrow -1} \frac{x^2 - x - 2}{x^3 - x}$

6. $\lim_{u \rightarrow -2} \sqrt{u^4 + 3u + 6}$

10. $\lim_{x \rightarrow 2} \frac{x^4 - 16}{x - 2}$

14. $\lim_{x \rightarrow 1} \frac{x^8 - 1}{x^5 - x}$