

Chapter 12 Review

ALL PROBLEMS MUST BE DONE ON SEPARATE PAPER OTHERWISE; THE REVIEW WILL NOT BE GRADED. SHOW ALL WORK FOR CREDIT. REVIEW IS DUE ON TEST DAY.

Evaluate the factorial expression.

1)  $\frac{8!}{6!} \frac{8!}{6!}$

Write out the first five terms of the sequence.

2)  $\{s_n\} = \{2(3n - 1)\}$

3)  $\{c_n\} = \left\{\frac{4^n}{n}\right\}$

The given pattern continues. Write down the  $n$ th term of the sequence  $\{a_n\}$  suggested by the pattern.

4)  $-1, 1, 3, 5, 7, \dots$

5)  $4, -8, 12, -16, \dots$

The sequence is defined recursively. Write the first four terms.

6)  $a_1 = 5; a_n = a_{n-1} - 2$

Write out the sum.

7)  $\sum_{k=1}^n (k+2)$

Express the sum using summation notation.

8)  $3^2 + 4^2 + 5^2 + \dots + 10^2$

Find the sum of the sequence.

9)  $\sum_{k=1}^5 k$

An arithmetic sequence is given. Find the common difference and write out the first four terms.

10)  $\{s_n\} = \{9 - 5n\}$

Find the  $n$ th term and the 8<sup>th</sup> term of the arithmetic sequence  $\{a_n\}$  whose initial term,  $a$ , and common difference,  $d$ , are given.

11)  $a_1 = 84; d = -10$

Find the indicated term of the arithmetic sequence.

12) The twenty-third term of the arithmetic sequence  $0, 10, 20, \dots$

Find the first term, the common difference, and give a recursive formula for the arithmetic sequence.

13) 7th term is 43; 15th term is 3

Find the sum.

14)  $1 + 2 + 3 + \dots + 264$

15)  $\sum_{n=1}^{44} (5n - 4)$

A geometric sequence is given. Find the common ratio and write out the first four terms.

16)  $\{s_n\} = \{3^n\}$

Determine whether the given sequence is arithmetic, geometric, or neither. If the sequence is arithmetic, find the common difference; if it is geometric, find the common ratio.

17)  $3, -9, 27, -81, 243, \dots$

Find the fifth term and the  $n$ th term of the geometric sequence whose initial term,  $a$ , and common ratio,  $r$ , are given.

18)  $a = 4; r = 5$

Find the indicated term of the geometric sequence.

19) 8th term of  $1, 2, 4, \dots$

Find the  $n$ th term  $\{a_n\}$  of the geometric sequence. When given,  $r$  is the common ratio.

20)  $7, 14, 28, 56, 112, \dots$

Find the fifth term and the  $n$ th term of the geometric sequence whose initial term,  $a$ , and common ratio,  $r$ , are given.

21)  $a_4 = 81; r = 3$

Use a graphing utility to find the sum of the geometric sequence. Round answer to two decimal places, if necessary.

22)

$$\sum_{k=1}^5 2(3)^k$$

Determine whether the infinite geometric series converges or diverges. If it converges, find its sum.

23)  $3 + 1 + \frac{1}{3} + \frac{1}{9} + \dots$

Use the Principle of Mathematical Induction to show that the statement is true for all natural numbers  $n$ .

24)  $2 + 5 + 8 + \dots + (3n - 1) = \frac{n}{2} (3n + 1)$

Evaluate the expression.

25)  $\binom{5}{3}$

Expand the expression using the Binomial Theorem.

26)  $(5x - 2)^4$

Use the Binomial Theorem to find the indicated coefficient or term.

27) The 3rd term in the expansion of  $(4x + 9)^3$