## Graphing Basic Inequalities Due Exam Day

## Graph $x=3$.

Step 1: Draw a circle on the number.
Step 2: Decide whether to fill in the circle.
 $I f>$ or $<$, leave empty. $I f \geqslant$ or $\leq$ fill in.
Step 3: Draw an arrow.

$I f<$ or $\leqslant$, draw arrow to left.
$I f>$ or $\geqslant$, draw arrow to the right.
Write the inequality shown by the graph.
Step 1: Write a variable and the number indicated by the circle.


Step 2: Look at the direction of the arrow. If arrow points left, use $<$ or $\leq$. If arrow points right, use $>$ or $\equiv$.
Step 3: Look at the circle.
If circle is empty, use $>$ or $<$.
If circle is filled in use, $\geqslant$ or $=$. $\quad x>-4$

## Graph each inequality.

5. $m \geq 8-3$
6. $p<3.5$


Write the inequality shown by the graph.
7.

8. $\underset{-8}{\mid} \underset{-7}{\mid} \mid$

## Graph each inequality.

5. $k>-12$
graph:
6. $b \leq 2^{3}-10$ graph:
7. $-6 \frac{1}{2} \leq w$
graph:
8. $n<-\sqrt{2(5)+6}$
graph:

Describe the solutions of each inequality in words.

1. $2 m \geq 6$
2. $t+3<8$
3. $1<x-5$ $\qquad$
4. $-10 \geq \frac{1}{2} c$ $\qquad$
Graph each inequality.
5. $x>-7$
6. $p \geq 2^{3}$

7. $4.5 \geq r$
8. $y<-\sqrt{14-5}$


Write the inequality shown by each graph.

11.

12.


## Define a variable and write an inequality for each situation. Graph the solutions.

13. Josephine sleeps more than 7 hours each night.

14. In 1955 , the minimum wage in the U.S. was $\$ 0.75$ per hour.

## Basic Inequalities



16. As of Aug. 1996, the speed limit on rural interstates in North Carolina is 70 mph .
17. In 2005 , the minimum wage in the U.S. was $\$ 5.15$ per hour.
Write the inequality shown by each graph.
Write the inequality shown by each graph.

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Solving inequalities is just like solving equations with ONE MAJOR DIFFERENCE. In inequalities, negative coefficients require a sign direction change!

The Rules:
-Use the same processes of isolating the variable as you would an equation.
-Inequalities with an equal sign included: do not drop or add "equal to" signs. This is a primary cause of wrong answers in inequalities; people forget and drop the equal sign.
-When you get to the final step of clearing out the coefficient

- If it is positive, you leave the sign alone.
olf it is negative, you change the direction of the sign. Flip the inequality!! That's it folks. Otherwise, it is just like equations.

| Examples: $2 x+4>3 x-2$ sam $-3 x \quad-3 x$ | nequality moving small $x$ value | $\begin{array}{ll} 2 x+4>3 x-2 \\ -2 x \quad-2 x \end{array}$ |
| :---: | :---: | :---: |
| $-\mathrm{x}+4>-2$ |  | +4> x -2 |
| -4 -4 |  | +2 +2 |
| $(-1)-x>\underline{-6(-1)}$ | No sign Change | $6>\mathrm{x}$ |
| SIGN CHANGE!!! x < 6 | is the same thing as | $6>x$ |
| ALWAYS CHECK YOUR ANSWER!!!!! | $\mathrm{X}<6$ PICK A NUMBER LESS THA | PICK ZERO) |
| $0<6$ TRUE |  | $6>0$ TRUE |



## Solve each inequality.

9. $v+1>v-6$
10. $3(x+4) \leq 3 x$
11. $-2(8-3 x) \geq 6 x+2$

## Word problems Inequalities

Write and solve an inequality for each problem.
9. A full-year membership to a gym costs $\$ 325$ upfront with no monthly charge. A monthly membership costs $\$ 100$ upfront and $\$ 30$ per month.
For what numbers of months is it less expensive to have a monthly membership?
10. The sum of the lengths of any two sides of a triangle must be greater than the length of the third side. What are the possible values of $x$ for this triangle?

12. Ian wants to promote his band on the Internet. Site A offers website hosting for $\$ 4.95$ per month with a $\$ 49.95$ startup fee. Site B offers website hosting for $\$ 9.95$ per month with no startup fee. For how many months would lan need to keep the website for Site B to be less expensive than Site A?
13. For what values of $x$ is the area of the rectangle greater than the perimeter?

- Graphing an inequality in $y+$ form is not that different than graphing an equation of the $y=m x+b$ form. First you locate the line of the graph as if it were $y=m x+b$, then you get fancy with it. Remember open circles were used when there was no = sign in your equality? Well, now you use a dotted (dashed0 line with open spaces between the dashes. AS solid line means it has an = sign also. Then you have to "shade" up for greater than, down for less than. Examples:



## What is up or down? <br> Put your ruler end on the line. If the ruler points to the top of the paper, that is up. If it points to the bottom of the paper, it is down.

## Solutions? Any point

 in the shaded area!!! If it is a solid line, also any point on the line (dotted line, those points don't count!!!!


Graph the following Inequalities


- Graphing a system of inequalities in $y+$ form is not that different than graphing a system of equations of the $y=m x+b$ form. First you locate both lines of the graph as if it were $y=m x+b$, then you get fancy with it. Remember open circles were used when there was no = sign in your equality? Well, now you use a dotted (dashed) line with open spaces between the dashes. AS solid line means it has an = sign also. Then you have to "shade" up for greater than, down for less than. Examples:
$Y<3 x+2$ and $y>1 / 2 x-3$

| Slope $=$ <br> $3 / 1$ | Y <br> intercep <br> $t=2$ | Slope <br> $=1 / 2$ | $Y$ <br> interce <br> $p t=-3$ |
| :--- | :--- | :--- | :--- |
| No equal <br> sign...dott <br> ed line | Less <br> than <br> shade <br> down | dotted | Shade <br> up |


| The solutions are |
| :--- |
| the points where |
| the two shaded |
| areas meet |
| (remember dotted |
| lines not included, |
| solid lines included) |

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Quick trick to test your graph. Use (0,0)
Put in both equations. If both are true, then $(0,0)$ is in solution area, if not it should be outside.
Right example $0<0+2$ True $0>0$-3 True $(0,0)$ IS IN solution area.
Left example $0>0-1 / 2$ True $0<0-2$ False $(0,0)$ is not in the solution set.


Graph the following System of Inequalities

$$
\begin{aligned}
& y \leq \frac{3}{4} x+1 \\
& y>-3 x-2
\end{aligned}
$$

## Name

$$
y \leq 2 x-3
$$

$$
y \geq 2 x+2
$$




