

**Algebra 1**  
**Lesson 8.5: Factoring Special Products**  
**Mrs. Snow, Instructor**

The ability to see a pattern can save you a lot of time and energy when you are factoring a polynomial.

**Vocabulary: Perfect Square** – a trinomial where the first and last terms are perfect squares and the middle term is 2 times the factor of the first term and last term.

There are 2 forms of a **perfect square**:

$$a^2 + 2ab + b^2 = (a + b)^2$$

$$a^2 - 2ab + b^2 = (a - b)^2$$

<p>Factor:</p> $  \begin{array}{c}  x^2 + 12x + 36 \\  \swarrow \quad \downarrow \quad \searrow \\  x \cdot x + 2(6)x + 6 \cdot 6 \\  \vdots \\  (x + 6)^2  \end{array}  $	<ol style="list-style-type: none"> <li>1. Is the first term a perfect square?</li> <li>2. Is the last term a perfect square?</li> <li>3. Linear term=2ab?</li> <li>4. So factor using the pattern of a perfect square.</li> </ol>
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Factor if possible:

$x^2 + 4x + 4$

$x^2 - 14x + 49$

$9x^2 - 6x + 4$

Another important polynomial pattern to remember is the **difference of two squares**. The term is self-describing, that is, it is what it is called: two terms that are perfect squares and are subtracted from each other.

$$a^2 - b^2 = (a + b)(a - b)$$

Factor:

$  \begin{array}{c}  x^2 - 16 \\  x^2 - 4^2 \\  (x + 4)(x - 4)  \end{array}  $	<ol style="list-style-type: none"> <li>1. First and last terms are perfect squares</li> <li>2. They are subtracted from each other.</li> <li>3. Factor per equation.</li> </ol>
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You try:

$x^2 - 25$

$x^2 - 49$

$4x^2 - 36$

A company produces square sheets of aluminum. Each has an area of  $(9x^2 + 6x + 1)m^2$ . The side length of each sheet is in the form of  $cx + d$ , where c and d are whole numbers. Find an expression in terms of x for the perimeter of a sheet. When  $x=3$  meters, what is the perimeter?