## Algebra I

## Lesson 2.6 - Rates, Ratios, and Proportions

Mrs. Snow, Instructor

Miles per hour, gallons per square foot, miles per gallon, teacher to student ratio, male to female ratio, win to loss. These relationships are ratios and are comparisons of two quantities that are divided. We can write ratios in a couple different ways: the ratio of $a$ to $b$ may be written as $a$ : $b$ or $\frac{a}{b}$ where $b \neq 0$.

## Vocabulary

Equivalent - ratios that are equal $\left(\frac{a}{b}=\frac{c}{d}\right)$, more specifically,
Proportion - a statement that has to equivalent ratios, that is: $\frac{1}{2}=\frac{5}{10}$
Rate - a ratio where the quantities have two different units: $\frac{58 \mathrm{mi}}{2 \mathrm{gal}}$
Unit rate - a rate written as "stuff" per single amount. You can convert any rate to a unit rate: $\frac{58 \mathrm{mi}}{2 \mathrm{gal}}=\frac{29 \mathrm{mi}}{1 \mathrm{gal}}$

|  | Denominator is a single unit |
| :---: | :---: |
| The ratio of games won to games lost for a baseball team is $3: 2$. If the team lost 12 games, how many did they win? $\begin{aligned} & \frac{\operatorname{win}}{\operatorname{loss}} \rightarrow \frac{3}{2} \\ & \frac{3}{2}=\frac{x}{12} \\ & 6(12) \frac{3}{2}=\frac{x}{12}(12) \\ & 18=x \end{aligned}$ <br> ans: 18 wins | 1. Write a ratio comparing sin to lost games <br> 2. Write a proportion. With $\mathbf{x}$ as the unknown number of wins. <br> 3. Solve for $x$ <br> 4. reduce before you multiply!! <br> 5. units!!! |
| Cory earned $\$ 52.50$ in 7 hours. Find the unit rate. (how much does he make per hour?) $\frac{\frac{52.50}{7}}{7.5}=\frac{x}{1}$ <br> ans: $\$ 7.50$ dollars per hour | 1. Write proportion to find an equivalent ratio with a denominator equal to 1. <br> 2. Well, we already have solved for $x$, so divide the left side of the equation! <br> 3. remember units!!!! |

Another way we can solve proportions is to cross multiply or use the Cross Product Property. In a proportion, the cross products are equal.

| $\frac{2}{3}=\frac{4}{6}$ |  |
| :--- | :--- |
| $(2)(6)=(4)(3)$ | 1. Draw an $X$ through your proportion; left side <br> numerator down to right side denominator and right |
| $12=12$ | side numerator down to left side denominator. <br> 2. Set the products equal to each other |

## Solve:

The ratio of cat to dog adoptions at an animal rescue shelter is $3: 4$. If 18 cats are adopted during the month of December, how many dogs were adopted?

The Keith went on a bike ride, according to the map he had gone 56 miles. He had only been on the road for 4 hours. What was his speed in miles per hour? What is the speed in feet/second? Round to the nearest tenth.

| $\frac{4}{7}=\frac{x}{42}$ | $-\frac{5}{2}=\frac{y}{8}$ | $\frac{g+3}{5}=\frac{7}{4}$ |
| :---: | :---: | :---: |
| $\frac{27}{x}=\frac{3}{8}$ | $\frac{2 w}{9}=\frac{10}{15}$ | $\frac{3}{x-5}=\frac{4}{8}$ |

A scale model of the human heart is 16 feet long. The scale is $32: 1$. How many inches long is the actual human heart?

