## Algebra II

## Lesson 3: Transformation Rules for Algebraic Equations <br> Mrs. Snow, Instructor

When a number is added or changed in an algebraic equation, a transformation will occur. The graph will be moved up or down, left or right, or be stretched or shrunk. These changes are known as transformations. When a parent function $f(x)$ is transformed, it becomes a different function. Let's use $t(x)$ for the transformed function.

| $f(x+h)$ | move the $x$-value $\boldsymbol{h}$ units left | graph will slide horizontally left |
| :---: | :---: | :---: |
| $f(x-h)$ | move the $x$-value $\boldsymbol{h}$ units right | graph will slide horizontally right |
| $a(f(x))$ | multiply the $y$-values by $\boldsymbol{a}$ | $a>0$ <br> vertical stretch/steeper or narrower <br> $0<a<1$ fraction vertical shrink/flatter or wider |
| $-f(x)$ | graph will flip upside down | Reflection across x -axis |
| $f(x)+k$ | move $y$-value $\boldsymbol{k}$ units up | Vertical translation up $k$ units |
| $f(x)-k$ | move $y$-value $\boldsymbol{k}$ units down | graph will slide vertically down $k$ units |
| Put it all together | $\boldsymbol{t}(\boldsymbol{x})=\boldsymbol{a} \cdot \boldsymbol{f}(\boldsymbol{x}-\mathrm{h})+\boldsymbol{k}$ |  |

Enter parent function into calculator, and then enter equation below, what happened?

| 1. $t(x)=2 x^{2}$ $t(x)=\frac{1}{4} x^{2}$ $t(x)=x^{2}+3$ <br> $t(x)=-x^{2}+3$    <br> 2. $\quad t(x)=x^{2}-3$ $t(x)=(x-3)^{2}$ $(x)=\left(x^{2}+3\right)$ $(x)=-\left(x^{2}+3\right)$ <br> 3. $\quad t(x)=2\|x\|$ $t(x)=\|x+2\|$ $t(x)=\|x\|+2$ $t(x)=-\|x\|+2$ <br> 4. $t(x)=\frac{5}{x}$ $t(x)=\frac{1}{x+4}$ $t(x)=\frac{1}{x}+3$ $t(x)=-\left(\frac{1}{x}+3\right)$ |
| :--- | :--- | :--- | :---: |

The order of operations for transformations is similar to those of equations; we deal with the multiplication before addition/subtraction. For graphs of functions involving more than one transformation, apply each change in the following order::

1. Horizontal Translation
2. Stretching or shrinking
3. Reflection
4. Vertical shift up/down

Example 1... Describe each combined transformation, in the correct order.

| a. $f(x-2)+3$ | b. $1 / 2 g(x)+3$ |
| :--- | :--- |
| c. $-2 g(x)-7$ | d. $3 h(x-4)+1$ |

When dealing with just a graph of a function, look at the $x$ - $y$ ordered pairs. For a horizontal shift, work with the $x$-value. For the stretch and vertical translations work with the $y$-value.

Example 2 Transform the function below to $h(x+4)-2$. Show each step.


