Algebra 2 Lesson 1-1, Part 2: Properties of Real Numbers

The set of real numbers consists of two subsets: the set of rational numbers and the set of irrational numbers. This set of numbers works with eight (8) properties that govern all operations.

Additive Identity Property

The sum of zero (0) and any number yields the original number eg.: 5+0=0.

Additive Inverse Property

The sum of a number and its opposite equals zero (0), eg.: 5 + (-5) = 0.

Multiplicative Identity Property

The product of any number and 1 equals the original number, eg.: $5 \cdot 1 = 5$.

Multiplicative Inverse Property

The product of a nonzero number and its reciprocal equals 1, eg: $5 \cdot \frac{1}{5} = 1$

Closure Property

The sum or product of any two real numbers is a real number, eg: $a + b \in R$, $a \cdot b \in R$

Commutative Property

You can add or multiply real numbers in any order and the answer remains the same, eg.: a + b = b + a, $a \cdot b = b \cdot a$

Associative Property

The sum or product of three or more real numbers is unchanged, regardless of the order the numbers are grouped, eg:

 $(a+b)+c = a + (b+c), \qquad (a \cdot b) \cdot c = a \cdot (b \cdot c)$

Distributive Property

When multiplying a sum by a number, the result is the same, whether you add first and then multiply or multiply each number first and then add the numbers, eg.: a(b + c) = ab + ac,

 $(b+c) \cdot a = ba + ca$